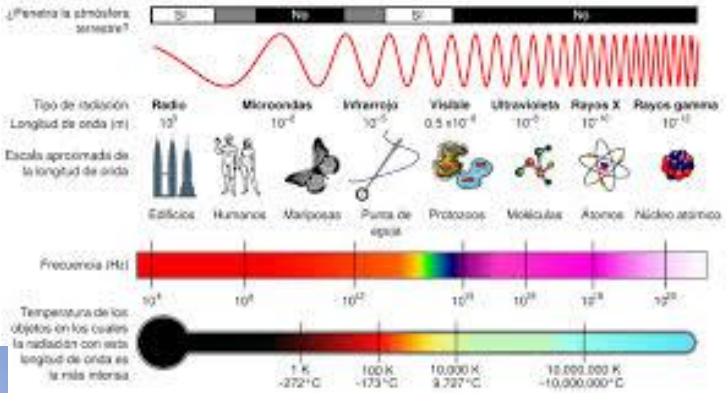
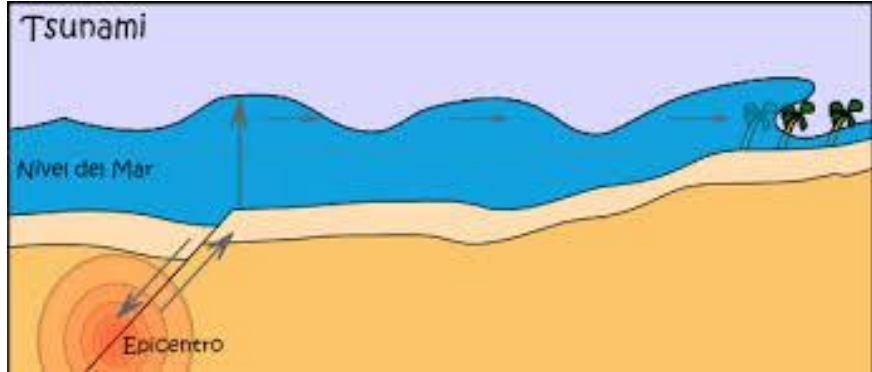
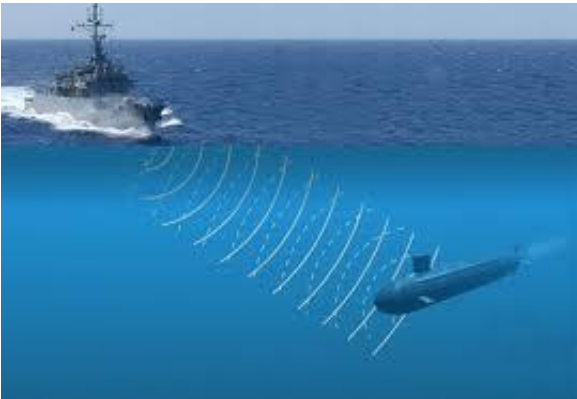


# Ondas

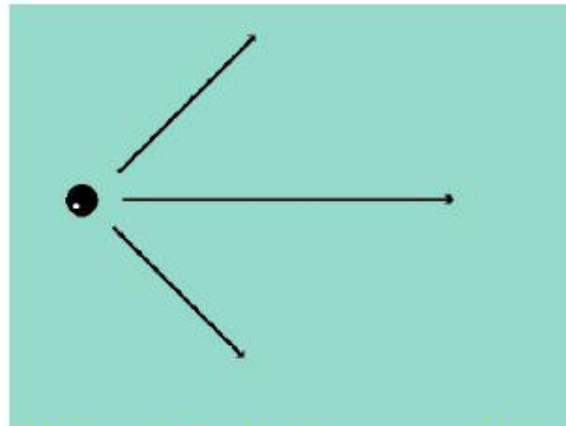


# Ondas

## Perturbaciones en un medio y su propagación



Medio en Equilibrio



Dirección de Propagación



Deformaciones

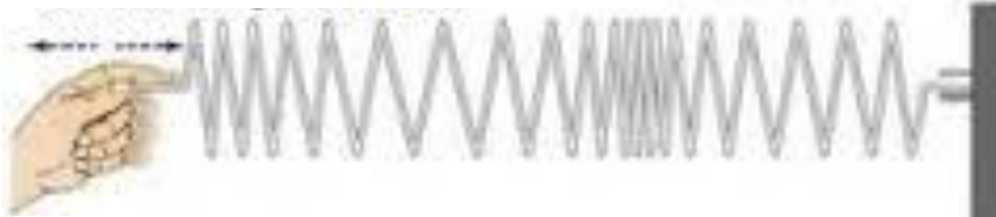
$$\vec{\epsilon} = \vec{\epsilon}(\vec{r}, t)$$

$$\vec{\epsilon}(\vec{r}, t) = \epsilon_x(xyz, t)\vec{i} + \epsilon_y(xyz, t)\vec{j} + \epsilon_z(xyz, t)\vec{k}$$

# Ondas

## Perturbaciones en un medio y su propagación

Ondas longitudinales



Ondas transversales

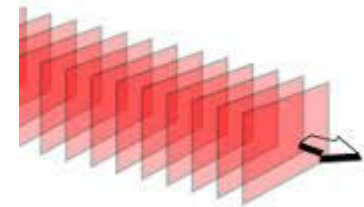
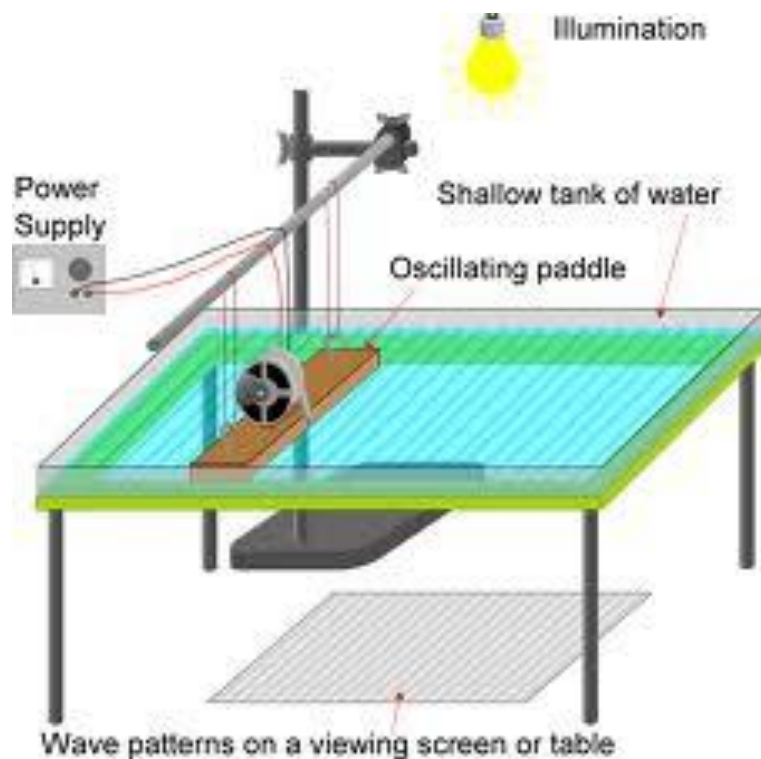


# Ondas

## Frentes de ondas: Plano

$$\vec{\epsilon} = \vec{\epsilon}(x, t)$$

$$\vec{\epsilon}(\vec{r}, t) = \epsilon_x(x, t)\vec{i} + \epsilon_y(x, t)\vec{j} + \epsilon_z(x, t)\vec{k}$$

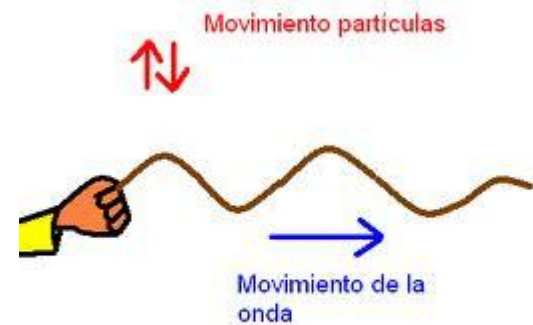
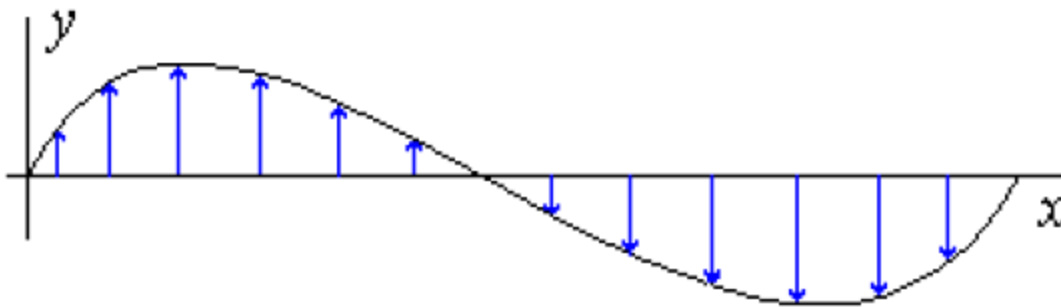


# Ondas

## Frentes de ondas: Plano

### Polarización lineal

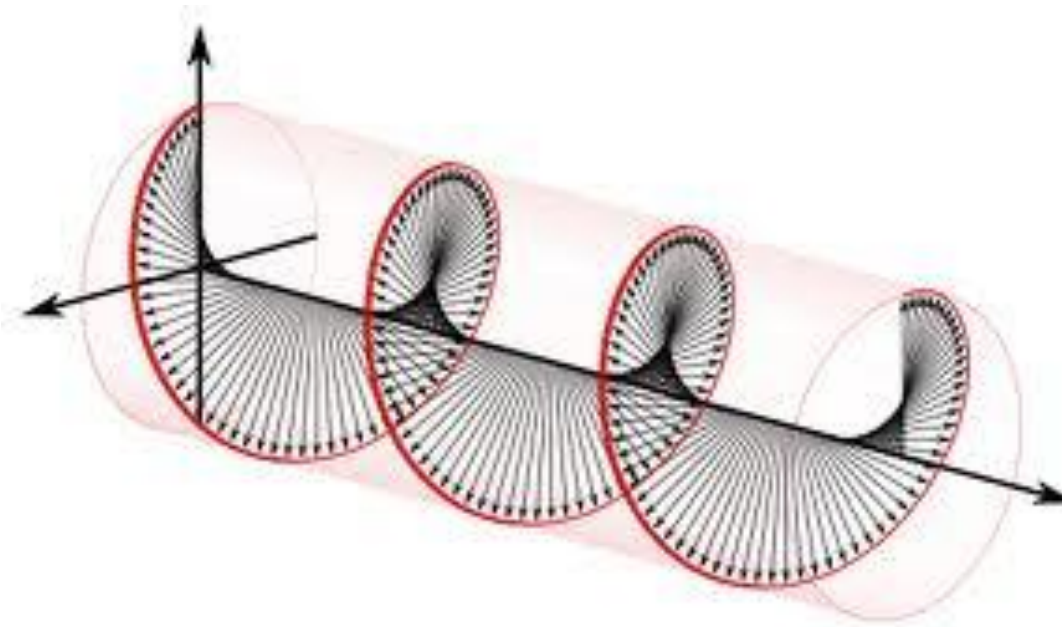
$$\vec{\epsilon} = \epsilon(x, t) \vec{j}$$



# Ondas

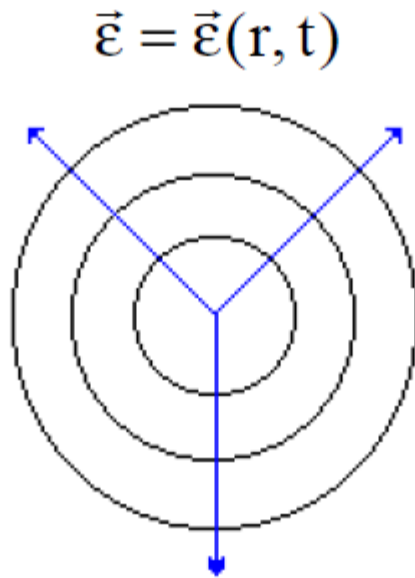
## Frentes de ondas: **Plano**

Polarización circular



# Ondas

## Frentes de ondas: Esférico





# Ondas

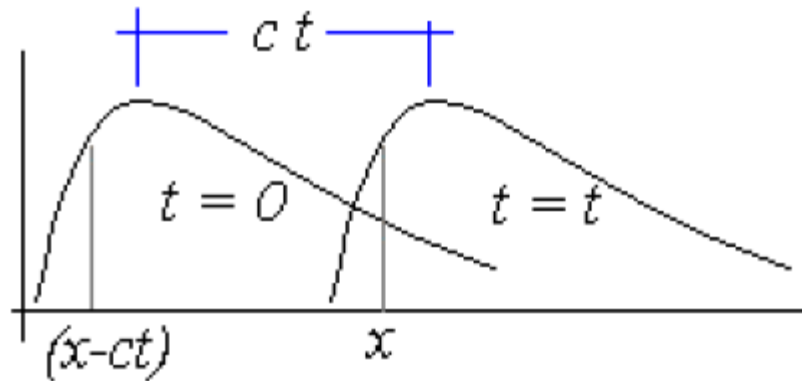
## Frentes de ondas: Circular





# Ondas

## Ecuación de las ondas



$$\varepsilon = \varepsilon(x - ct) \quad \rightarrow$$

$$\varepsilon = \varepsilon(x + ct) \quad \leftarrow$$

Definiendo la variable:

$$\xi = x \pm ct$$

Podemos escribir la perturbación de manera general como

$$\varepsilon = \varepsilon(\xi)$$

# Ondas

## Ecuación de las ondas

Derivando respecto de x

$$\frac{\partial \varepsilon}{\partial x} = \frac{\partial \varepsilon}{\partial \xi} \frac{\partial \xi}{\partial x} = \frac{\partial \varepsilon}{\partial \xi}$$

$$\frac{\partial^2 \varepsilon}{\partial x^2} = \frac{\partial}{\partial \xi} \left( \frac{\partial \varepsilon}{\partial x} \right) \frac{\partial \xi}{\partial x} = \frac{\partial}{\partial \xi} \left( \frac{\partial \varepsilon}{\partial \xi} \right) = \frac{\partial^2 \varepsilon}{\partial \xi^2}$$

Derivando respecto de t

$$\frac{\partial \varepsilon}{\partial t} = \frac{\partial \varepsilon}{\partial \xi} \frac{\partial \xi}{\partial t} = \pm c \frac{\partial \varepsilon}{\partial \xi}$$

$$\begin{aligned} \frac{\partial^2 \varepsilon}{\partial t^2} &= \frac{\partial}{\partial \xi} \left( \frac{\partial \varepsilon}{\partial t} \right) \frac{\partial \xi}{\partial t} \\ &= \frac{\partial}{\partial \xi} \left( \pm c \frac{\partial \varepsilon}{\partial \xi} \right) (\pm c) = c^2 \frac{\partial^2 \varepsilon}{\partial \xi^2} \end{aligned}$$

$$\frac{\partial^2 \varepsilon}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 \varepsilon}{\partial t^2} = 0$$

# Ondas

## Ecuación de las ondas

$$\frac{\partial^2 \varepsilon}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 \varepsilon}{\partial t^2} = 0$$



$$\nabla^2 \vec{\varepsilon} - \frac{1}{c^2} \frac{\partial^2 \vec{\varepsilon}}{\partial t^2} = 0$$

$$\nabla^2 \varepsilon_x - \frac{1}{c^2} \frac{\partial^2 \varepsilon_x}{\partial t^2} = 0$$

$$\nabla^2 \varepsilon_y - \frac{1}{c^2} \frac{\partial^2 \varepsilon_y}{\partial t^2} = 0$$

$$\nabla^2 \varepsilon_z - \frac{1}{c^2} \frac{\partial^2 \varepsilon_z}{\partial t^2} = 0$$

# Ondas

## Ecuación de las ondas

### Ecuación de Navier–Stokes (fluido incompresible)

$$\rho \left( \frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v} \right) = -\nabla p + \mu \nabla^2 \mathbf{v} + \mathbf{f}.$$

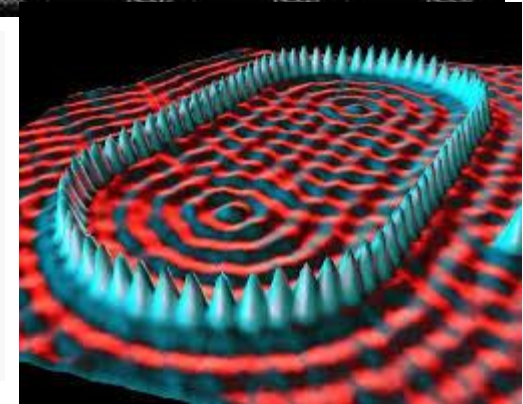
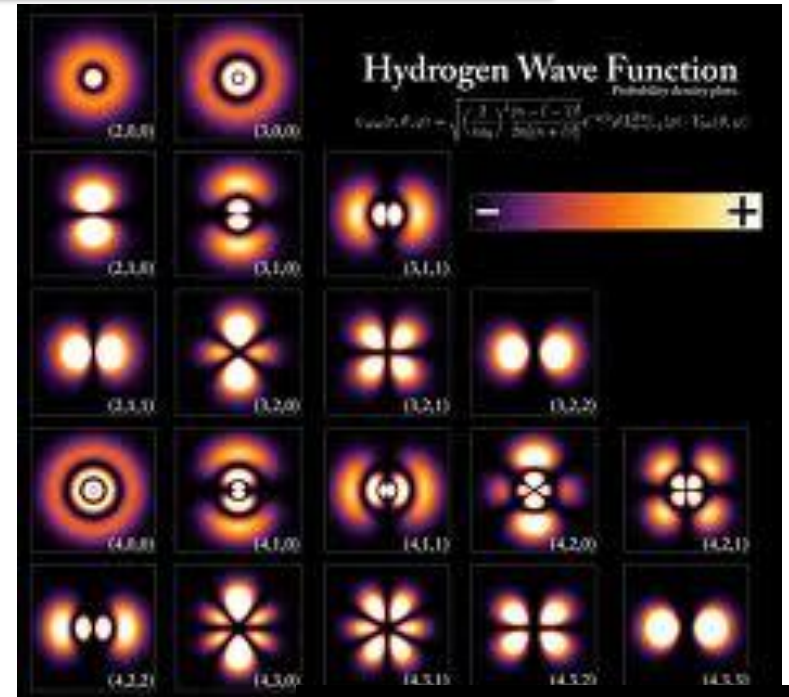
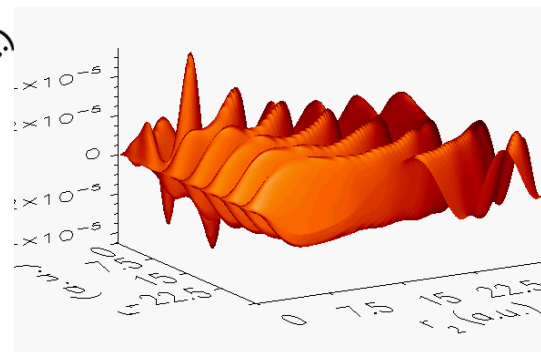
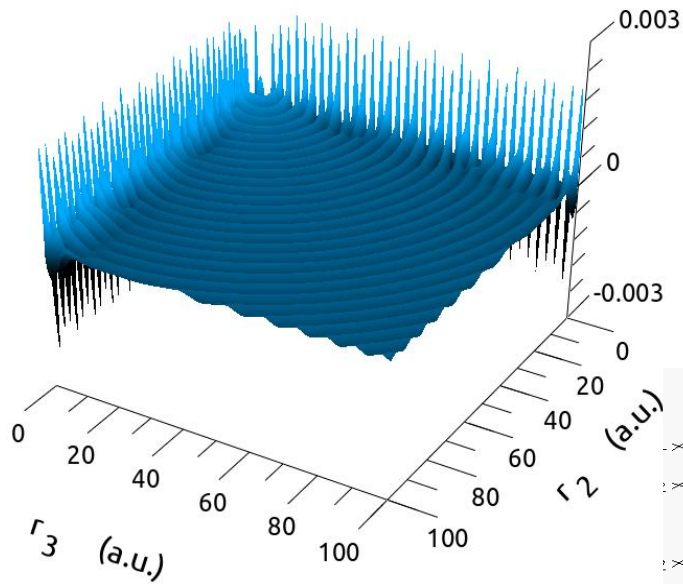


# Ondas

## Ecuación de las ondas

### Ecuación de Schrödinger

$$\left[ \frac{-\hbar^2}{2m} \nabla^2 + V \right] \Psi = i \hbar \frac{\partial}{\partial t} \Psi$$



# Ondas

## Ecuación de las ondas

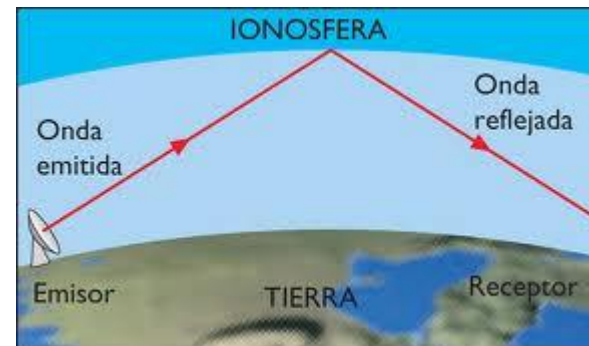
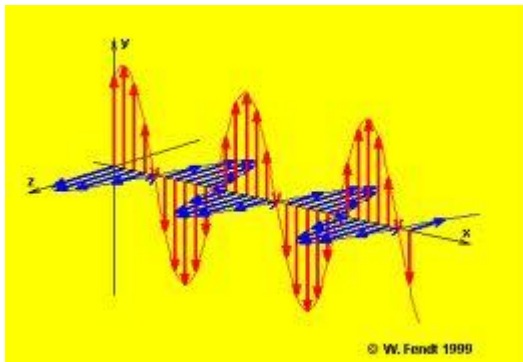
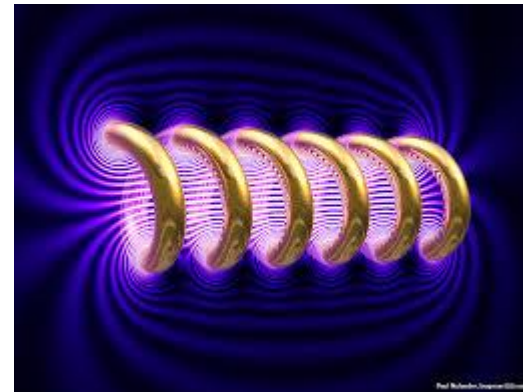
### Ecuaciones de Maxwell

$$\nabla \cdot \mathbf{D} = \rho$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

$$\nabla \times \mathbf{H} = \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t}$$



# Ondas

## Ondas Sinusoidales

$$\varepsilon = \varepsilon_0 \text{sen}(kx - \omega t)$$



$$\frac{\omega}{k} = c$$

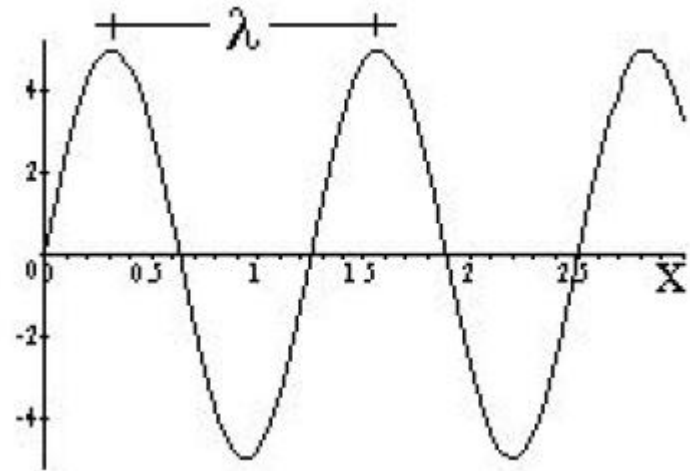


$$\varepsilon = \varepsilon_0 \text{sen } k(x - ct)$$

Para un momento particular del tiempo (que podemos elegir sin inconvenientes que sea  $t=0$ )

$$\lambda = \frac{2\pi}{k} \quad \longrightarrow \quad k = \frac{2\pi}{\lambda}$$

número de onda





# Ondas

## Ondas Sinusoidales

$$\varepsilon = \varepsilon_0 \operatorname{sen}(-\omega t) = -\varepsilon_0 \operatorname{sen}(\omega t)$$

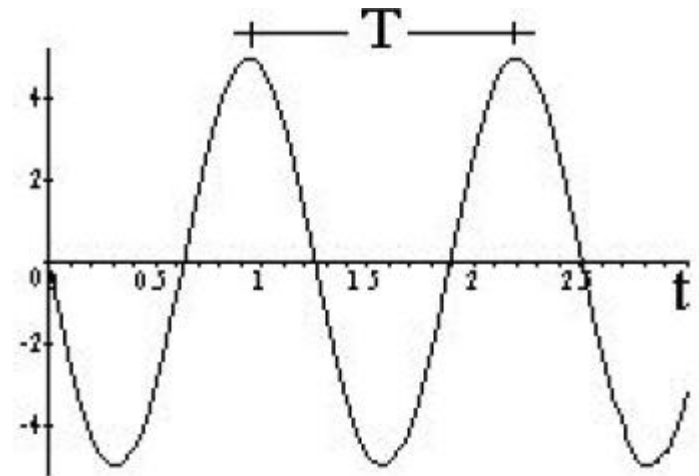
$$\varepsilon_0 \operatorname{sen}(\omega t) = \varepsilon_0 \operatorname{sen} \omega(t + T)$$

$$T = \frac{2\pi}{\omega}$$

frecuencia angular

$$\omega = \frac{2\pi}{T}$$

Para un punto espacial particular (que podemos elegir sin inconvenientes que sea  $x=0$ )



# Ondas

## Ondas Sinusoidales

frecuencia

$$\lambda \nu = c$$

$$\lambda = \frac{c}{\nu}$$

$$\varepsilon = \varepsilon_0 \operatorname{sen} \frac{2\pi}{\lambda} (x - ct)$$

$$\varepsilon = \varepsilon_0 \operatorname{sen} \frac{2\pi}{T} \left( \frac{x}{c} - t \right)$$

$$\varepsilon = \varepsilon_0 \operatorname{sen} 2\pi \nu \left( \frac{x}{c} - t \right)$$