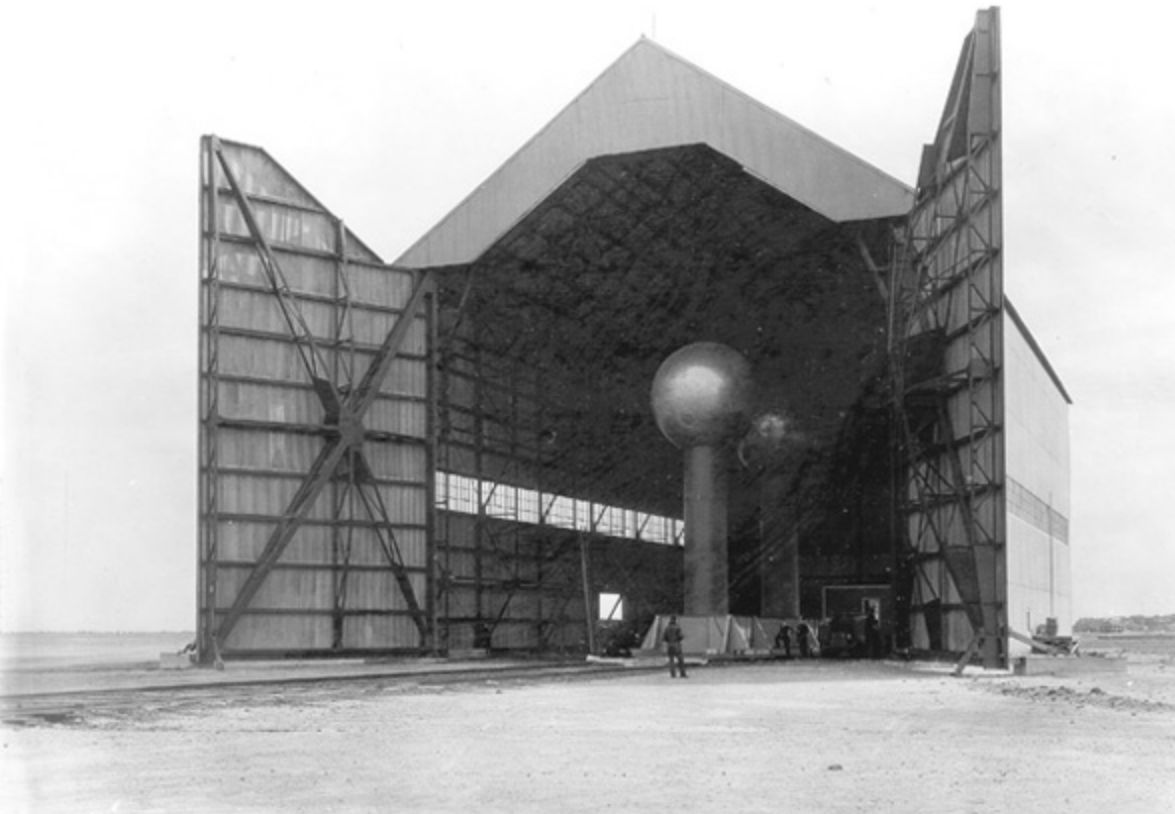


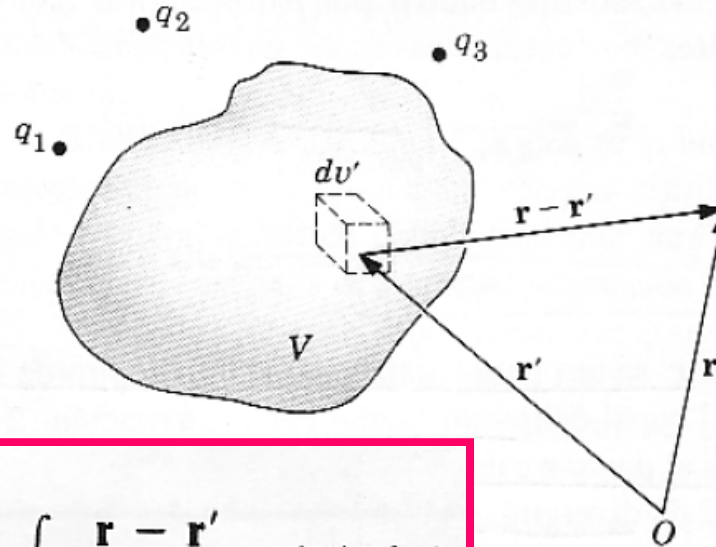
Electricidad



Generador de Van der Graff

Repaso

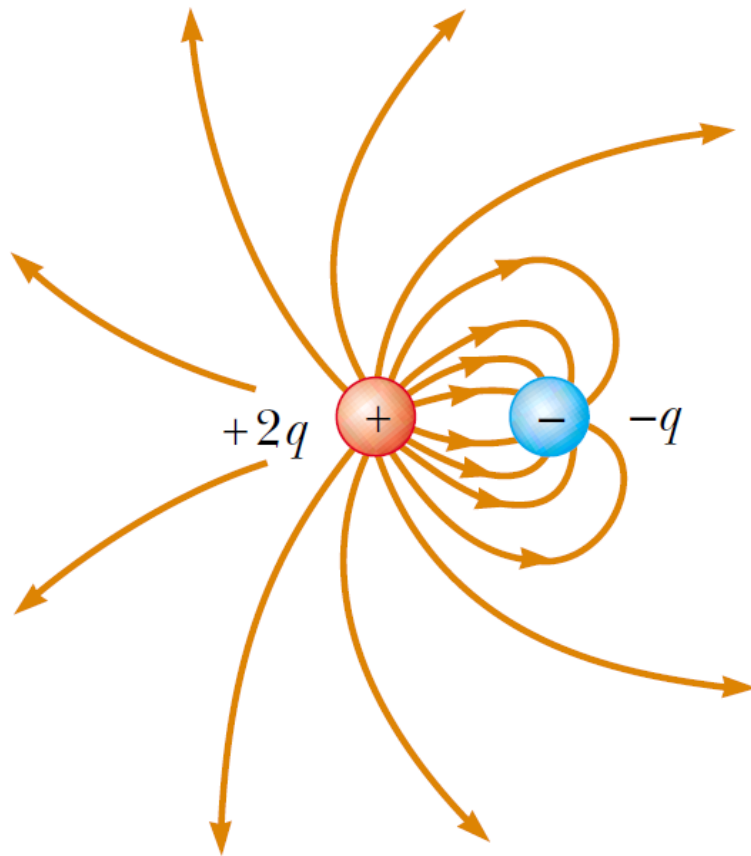
$$\mathbf{E} = \lim_{q \rightarrow 0} \frac{\mathbf{F}_q}{q}$$



$$\mathbf{E}(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \sum_{i=1}^N q_i \frac{\mathbf{r} - \mathbf{r}_i}{|\mathbf{r} - \mathbf{r}_i|^3} + \frac{1}{4\pi\epsilon_0} \int_V \frac{\mathbf{r} - \mathbf{r}'}{|\mathbf{r} - \mathbf{r}'|^3} \rho(\mathbf{r}') dv' + \frac{1}{4\pi\epsilon_0} \int_S \frac{\mathbf{r} - \mathbf{r}'}{|\mathbf{r} - \mathbf{r}'|^3} \sigma(\mathbf{r}') da'$$

El campo eléctrico es una propiedad de la distribución de carga y no representa una “interacción”.

Líneas de Fuerza



**Las líneas de fuerza
NO REPRESENTAN
TRAYECTORIAS**

**Las líneas de fuerza
NO PUEDEN CRUZARSE**

Experimento de Millikan (1909-1913)



(1868-1953)



THE
PHYSICAL REVIEW

THE ISOLATION OF AN ION, A PRECISION MEASURE-
MENT OF ITS CHARGE, AND THE CORRECTION
OF STOKES'S LAW.¹

BY R. A. MILLIKAN.

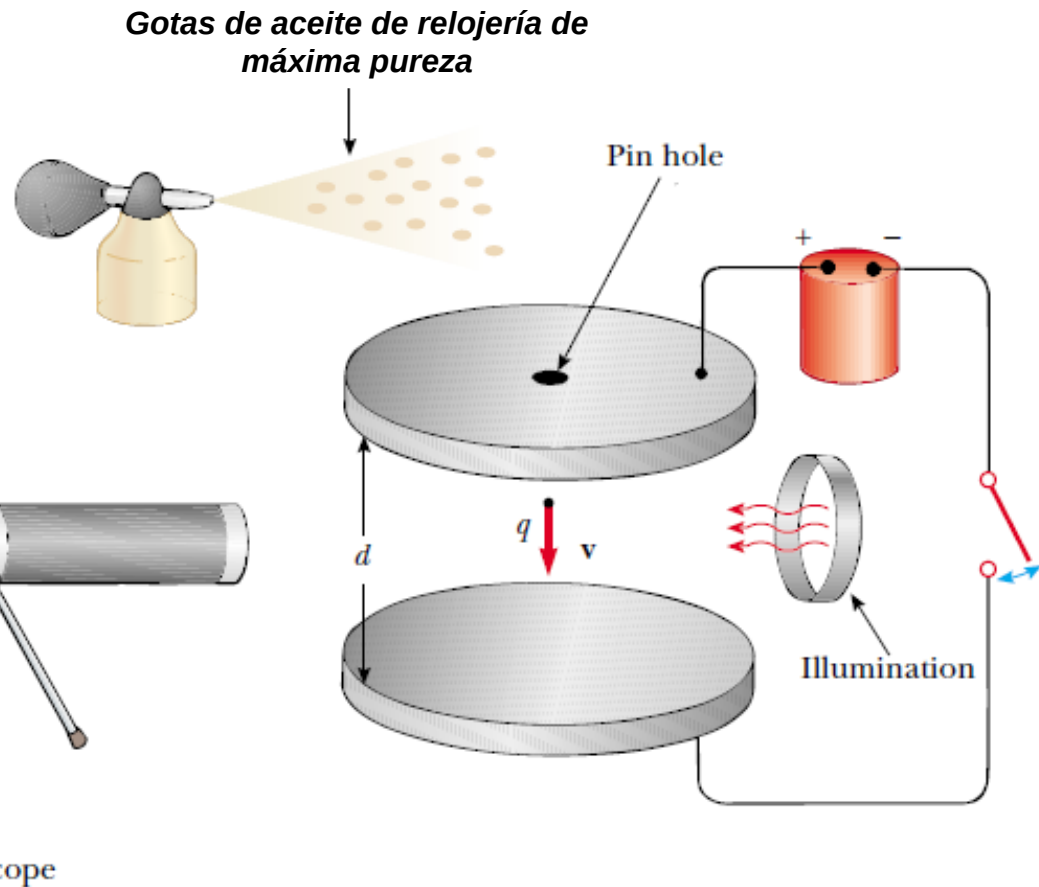
§ I. INTRODUCTION.

IN a preceding paper² a method of measuring the elementary electrical charge was presented which differed essentially from methods which had been used by earlier observers only in that all of the measurements from which the charge was deduced were made

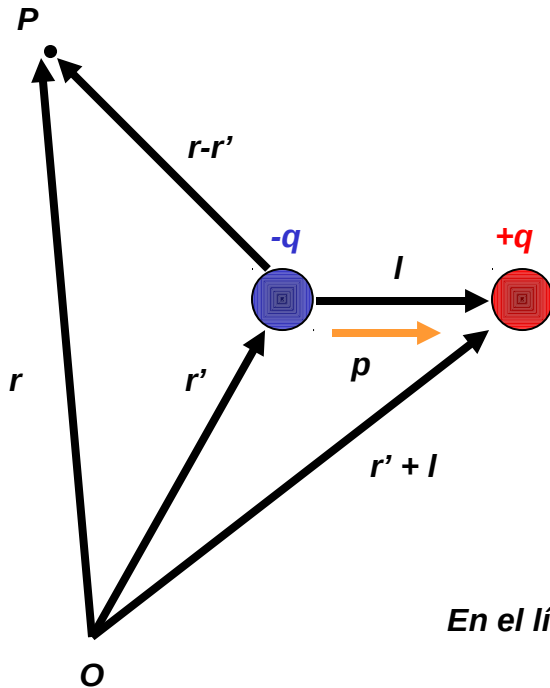
Experimento de Millikan



Harvey Fletcher
(1884-1981)



Dipolo Eléctrico



En el límite $l/r \ll 1$

$$\mathbf{E}(\mathbf{r}) = \frac{q}{4\pi\epsilon_0} \left\{ \frac{\mathbf{r} - \mathbf{r}' - \mathbf{l}}{|\mathbf{r} - \mathbf{r}' - \mathbf{l}|^3} - \frac{\mathbf{r} - \mathbf{r}'}{|\mathbf{r} - \mathbf{r}'|^3} \right\}$$

$$\begin{aligned} |\mathbf{r} - \mathbf{r}' - \mathbf{l}|^{-3} &= [(\mathbf{r} - \mathbf{r}')^2 - 2(\mathbf{r} - \mathbf{r}') \cdot \mathbf{l} + l^2]^{-3/2} \\ &= |\mathbf{r} - \mathbf{r}'|^{-3} \left[1 - \frac{2(\mathbf{r} - \mathbf{r}') \cdot \mathbf{l}}{|\mathbf{r} - \mathbf{r}'|^2} + \frac{l^2}{|\mathbf{r} - \mathbf{r}'|^2} \right]^{-3/2} \end{aligned}$$

$$|\mathbf{r} - \mathbf{r}' - \mathbf{l}|^{-3} = |\mathbf{r} - \mathbf{r}'|^{-3} \left\{ 1 + \frac{3(\mathbf{r} - \mathbf{r}') \cdot \mathbf{l}}{|\mathbf{r} - \mathbf{r}'|^2} + \dots \right\}$$

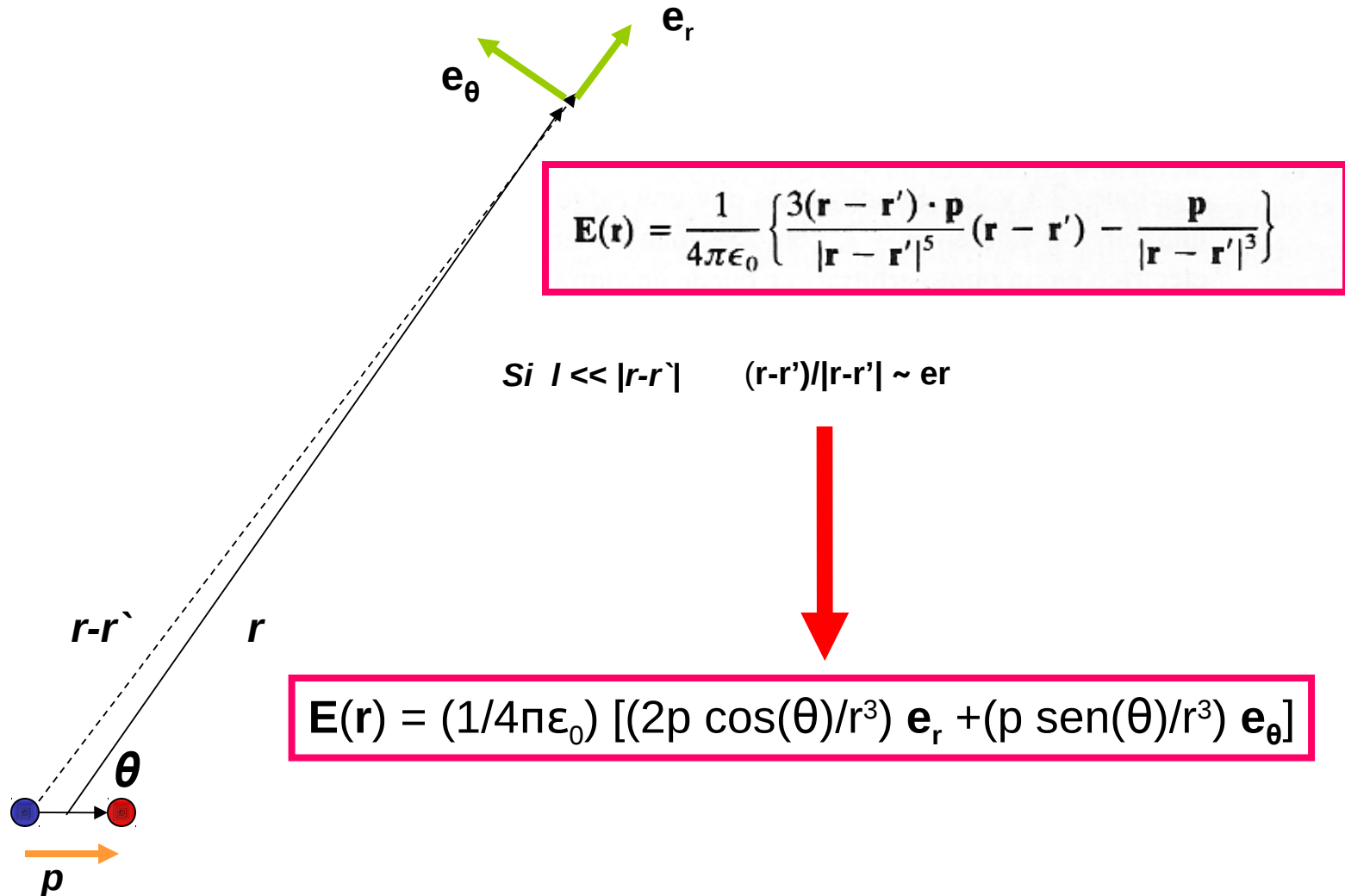
$$\mathbf{E}(\mathbf{r}) = \frac{q}{4\pi\epsilon_0} \left\{ \frac{3(\mathbf{r} - \mathbf{r}') \cdot \mathbf{l}}{|\mathbf{r} - \mathbf{r}'|^5} (\mathbf{r} - \mathbf{r}') - \frac{\mathbf{l}}{|\mathbf{r} - \mathbf{r}'|^3} + \dots \right\}$$

Se define el Momento Dipolar Eléctrico $\mathbf{p} = q\mathbf{l}$


$$\mathbf{E}(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \left\{ \frac{3(\mathbf{r} - \mathbf{r}') \cdot \mathbf{p}}{|\mathbf{r} - \mathbf{r}'|^5} (\mathbf{r} - \mathbf{r}') - \frac{\mathbf{p}}{|\mathbf{r} - \mathbf{r}'|^3} \right\}$$

El campo eléctrico del dipolo varía como $1/r^3$

Dipolo Eléctrico



Potencial Eléctrico

$$\left. \begin{aligned} \mathbf{E} &= -\nabla V \\ \nabla \times \mathbf{E} &= 0 \end{aligned} \right\}$$


CAMPO CONSERVATIVO

$$\left. \begin{aligned} \mathbf{F} &= -\nabla U \end{aligned} \right\}$$

Fuerza conservativa Energía potencial conservativa

Es fácil verificar esto para carga puntual y coord. cartesianas

$$\int \mathbf{E} \cdot d\mathbf{l} = -\int \nabla V \cdot d\mathbf{l}$$

$$V(\mathbf{r}) = -\int_{\text{ref}}^{\mathbf{r}} \mathbf{E} \cdot d\mathbf{l}$$